

# Package ‘LogRegEquiv’

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**Title** Logistic Regression Equivalence

**Description** Tools for assessing equivalence of similar Logistic Regression models.

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beta_equivalence	<i>beta_equivalence function</i>
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**Description**

This function takes two logistic regression models  $M_A, M_B$ , sensitivity level  $\delta_\beta$  and significance level  $\alpha$ . It checks whether the coefficient vectors are equivalent.

**Usage**

```
beta_equivalence(model_a, model_b, delta, alpha)
```

**Arguments**

model_a	logistic regression model $M_A$
model_b	logistic regression model $M_B$
delta	equivalence sensitivity level $\delta_\beta$ . This could either be a scalar or a vector with length matching the number of coefficients.
alpha	significance level $\alpha$

**Value**

equivalence	are the coefficient vectors equivalent? (boolean)
test_statistic	Equivalence test statistic
critical_value	a level- $\alpha$ critical value
ncp	non-centrality parameter
p_value	P-value

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brier_score	<i>brier_score function</i>
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**Description**

This function takes a observations vector  $y$  and matching predictions vector  $\pi$ . It returns the Brier score for the predictions. Unless specified otherwise, input containing NAs will result with an NA.

**Usage**

```
brier_score(y, pi, na.rm = FALSE)
```

**Arguments**

y	the observations vector
pi	the predictions vector
na.rm	ignore NA? (optional)

**Value**

The Brier score  $\frac{1}{N} \sum_{i=1}^N (y_i - \pi_i)^2$

**Examples**

```
brier_score(rbinom(10,1,seq(0.1, 1, 0.1)), seq(0.1, 1, 0.1))
```

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descriptive\_equiv      *descriptive\_equiv function*

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**Description**

This function takes two datasets  $X_A, X_B$ , regression formula, significance level  $\alpha$  and sensitivity level  $\delta_\beta$  (either vector or scalar). It builds a logistic regression model for each of the datasets and then checks whether the obtained coefficient vectors are equivalent, using the beta\_equivalence function.

**Usage**

```
descriptive_equiv(data_a, data_b, formula, delta, alpha = 0.05)
```

**Arguments**

data_a	dataset $X_A$ for model $M_A$
data_b	dataset $X_B$ for model $M_B$
formula	logistic regression formula
delta	equivalence sensitivity level $\delta_\beta$
alpha	significance level $\alpha$ (defaults to 0.05)

**Value**

equivalence the beta\_equivalence function output  
 model\_a logistic regression model  $M_A$   
 model\_b logistic regression model  $M_B$

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individual\_predictive\_equiv  
*individual\_predictive\_equiv function*

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### Description

This function takes two logistic regression models  $M_A, M_B$ , test data, significance level  $\alpha$  and allowed flips ratio  $r$ . It checks whether the models produce equivalent log-odds for the given test set and returns various figures.

### Usage

```
individual_predictive_equiv(model_a, model_b, test_data, r = 0.1, alpha = 0.05)
```

### Arguments

model_a	logistic regression model $M_A$
model_b	logistic regression model $M_B$
test_data	testing dataset
r	ratio of allowed 'flips' (defaults to 0.1)
alpha	significance level $\alpha$ (defaults to 0.05)

### Value

equivalence Are models  $M_A, M_B$  producing equivalent log-odds for the given test data? (boolean)  
test\_statistic The test statistic  
critical\_value a level- $\alpha$  critical value the test  
xi\_bar Mean  $\xi$  value for the test  
delta\_theta Calculated equivalence parameter  
p\_value P-value

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performance\_equiv      *performance\_equiv function*

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### Description

This function takes two logistic regression models  $M_A, M_B$ , test data, significance level  $\alpha$  and acceptable score degradation  $\delta_B$ . It checks whether the models perform equivalently on the test set and returns various figures.

**Usage**

```
performance_equiv(
  model_a,
  model_b,
  test_data,
  dv_index,
  delta_B = 1.1,
  alpha = 0.05
)
```

**Arguments**

model_a	logistic regression model $M_A$
model_b	logistic regression model $M_B$
test_data	testing dataset
dv_index	column number of the dependent variable
delta_B	acceptable score degradation (defaults to 1.1)
alpha	significance level $\alpha$ (defaults to 0.05)

**Value**

equivalence Are models  $M_A, M_B$  producing equivalent Brier scores for the given test data?  
(boolean)

brier\_score\_ac  $M_A$  Brier score on the testing data

brier\_score\_bc  $M_B$  Brier score on the testing data

diff\_sd\_l SD of the lower Brier difference  $BS^A - \delta_B^2 BS^B$

diff\_sd\_u SD of the upper Brier difference  $BS^A - \delta_B^{-2} BS^B$

test\_stat\_l  $t_L$  equivalence boundary for the test

test\_stat\_u  $t_U$  equivalence boundary for the test

crit\_val a level- $\alpha$  critical value for the test

delta\_B Calculated equivalence parameter

p\_value\_l P-value for  $t_L$

p\_value\_u P-value for  $t_U$

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ptg\_stud\_data

*Student Performance Data Set*

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### Description

Data from a student achievement in secondary education of two Portuguese schools. Full attribute description could be found in the source webpage.

### Usage

ptg\_stud\_data

### Format

An object of class `data.frame` with 649 rows and 31 columns.

### Details

The data used is taken from the Student Performance Data. The original data consists of 30 covariates (13 binary, 11 ordinal, 4 categorical, 2 numerical) and a numerical output variable indicating the students final grade in Portuguese Language course.

The data was split by gender (F/M)  $n_f = 383, n_m = 266$ . The target variable G3 was converted to binary, `final_fail` which indicates the cases where  $G3 < 10$ .

Next, each sub-population was divided into training and testing data, using a 4:1 ratio.

### Source

<https://archive.ics.uci.edu/ml/datasets/student+performance>

### References

P. Cortez and A. Silva. Using Data Mining to Predict Secondary School Student Performance. In A. Brito and J. Teixeira Eds., Proceedings of 5th FUTURE BUSINESS TECHNOLOGY CONFERENCE (FUBUTEC 2008) pp. 5-12, Porto, Portugal, April, 2008, EUROSIS, ISBN 978-9077381-39-7.

### See Also

<http://www3.dsi.uminho.pt/pcortez/student.pdf>

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*ptg\_stud\_f\_test*      *Student Performance Data Set - female testing data*

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**Description**

Student Performance Data Set - female testing data

**Usage**

`ptg_stud_f_test`

**Format**

An object of class `data.frame` with 77 rows and 30 columns.

**See Also**

`ptg_stud_data`

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*ptg\_stud\_f\_train*      *Student Performance Data Set - female training data*

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**Description**

Student Performance Data Set - female training data

**Usage**

`ptg_stud_f_train`

**Format**

An object of class `data.frame` with 306 rows and 30 columns.

**See Also**

`ptg_stud_data`

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ptg\_stud\_m\_test      *Student Performance Data Set - male testing data*

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**Description**

Student Performance Data Set - male testing data

**Usage**

ptg\_stud\_m\_test

**Format**

An object of class `data.frame` with 53 rows and 30 columns.

**See Also**

ptg\_stud\_data

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ptg\_stud\_m\_train      *Student Performance Data Set - male training data*

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**Description**

Student Performance Data Set - male training data

**Usage**

ptg\_stud\_m\_train

**Format**

An object of class `data.frame` with 213 rows and 30 columns.

**See Also**

ptg\_stud\_data



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`sigmoid`*Sigmoid function*

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**Description**

This function takes a number  $\theta$  and returns its respective sigmoid probability  $\frac{e^{\theta}}{1+e^{\theta}}$ . This is used in logistic regression to model  $P(y = 1|x)$ .

**Usage**

```
sigmoid(theta)
```

**Arguments**

`theta`            the linear predictor

**Value**

the sigmoid probability

**Examples**

```
sigmoid(0)
```

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